

# Estimating aerosol emissions from variational assimilation

N. Huneeus <sup>(1)</sup>, F. Chevallier <sup>(1)</sup>  
and O. Boucher <sup>(2)</sup>

(1) Laboratoire des Sciences du Climat et de l'Environnement, France

(2) Met Office, Hadley Centre, Exeter, United Kingdom



# Variational assimilation



$$J = (x - x_b)^T B^{-1} (x - x_b) + (y - H[x])^T R^{-1} (y - H[x])$$



We aim to minimize J !

J: Cost function

x: Control vector

$x_b$ : Background vector

y: observation vector

H: Transport model

B,R: Covariance error  
matrices



$$x^{n+1} = x^n - \alpha \nabla_x J(x^n)$$



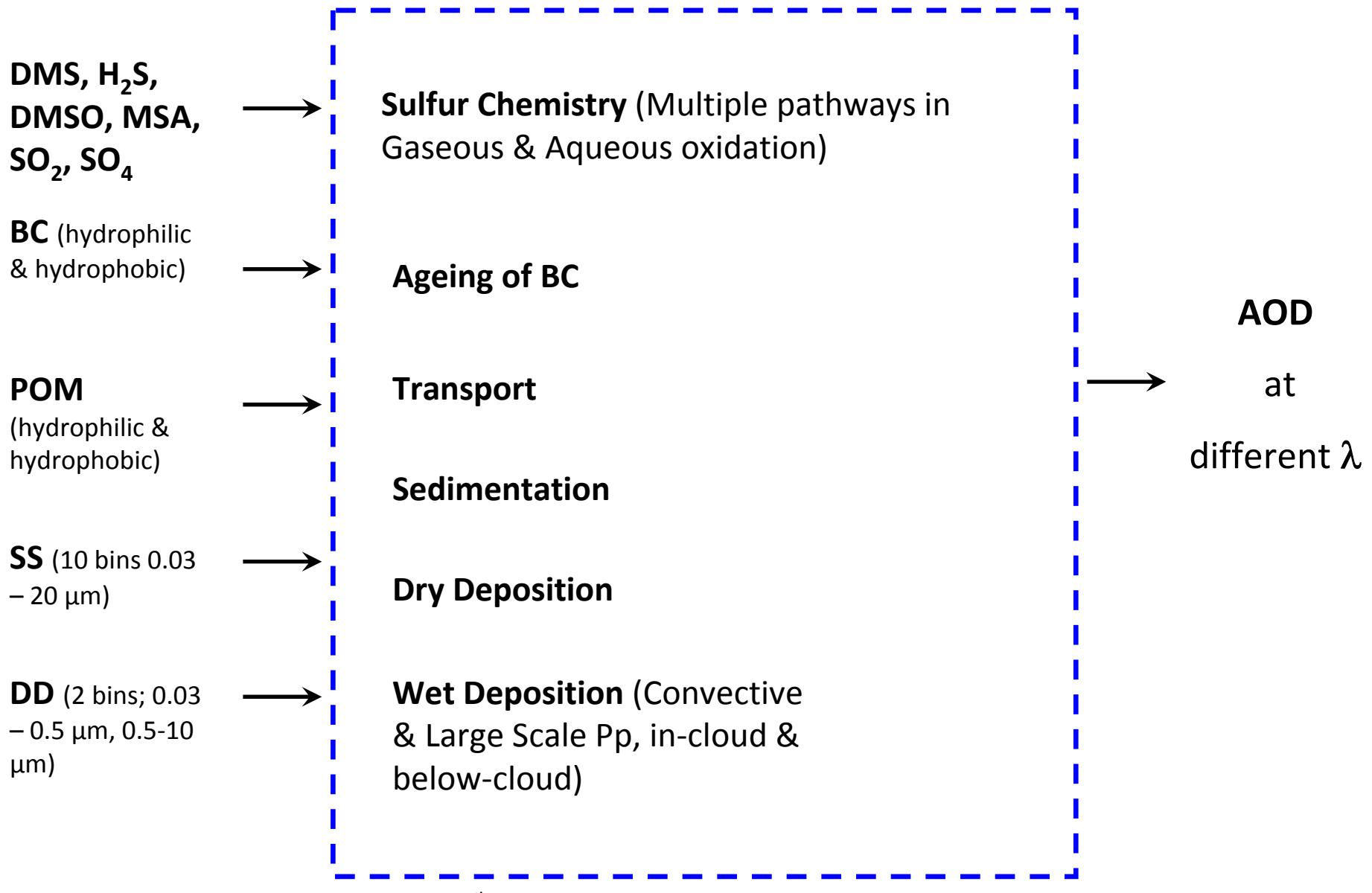
## Adjoint Method

$$\nabla_X J = H' * \nabla_Y J$$

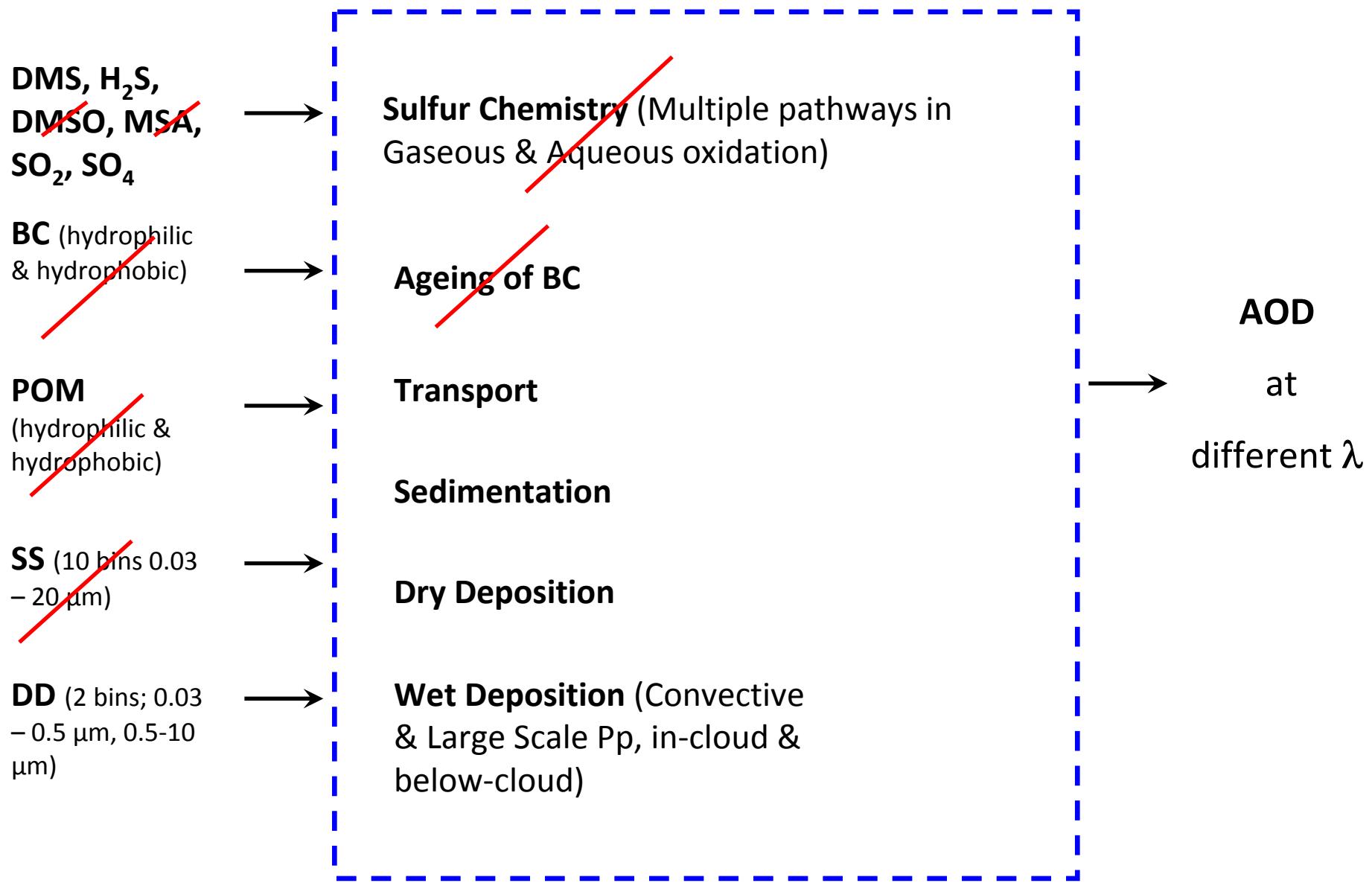


Computation of  
the gradient of  
J

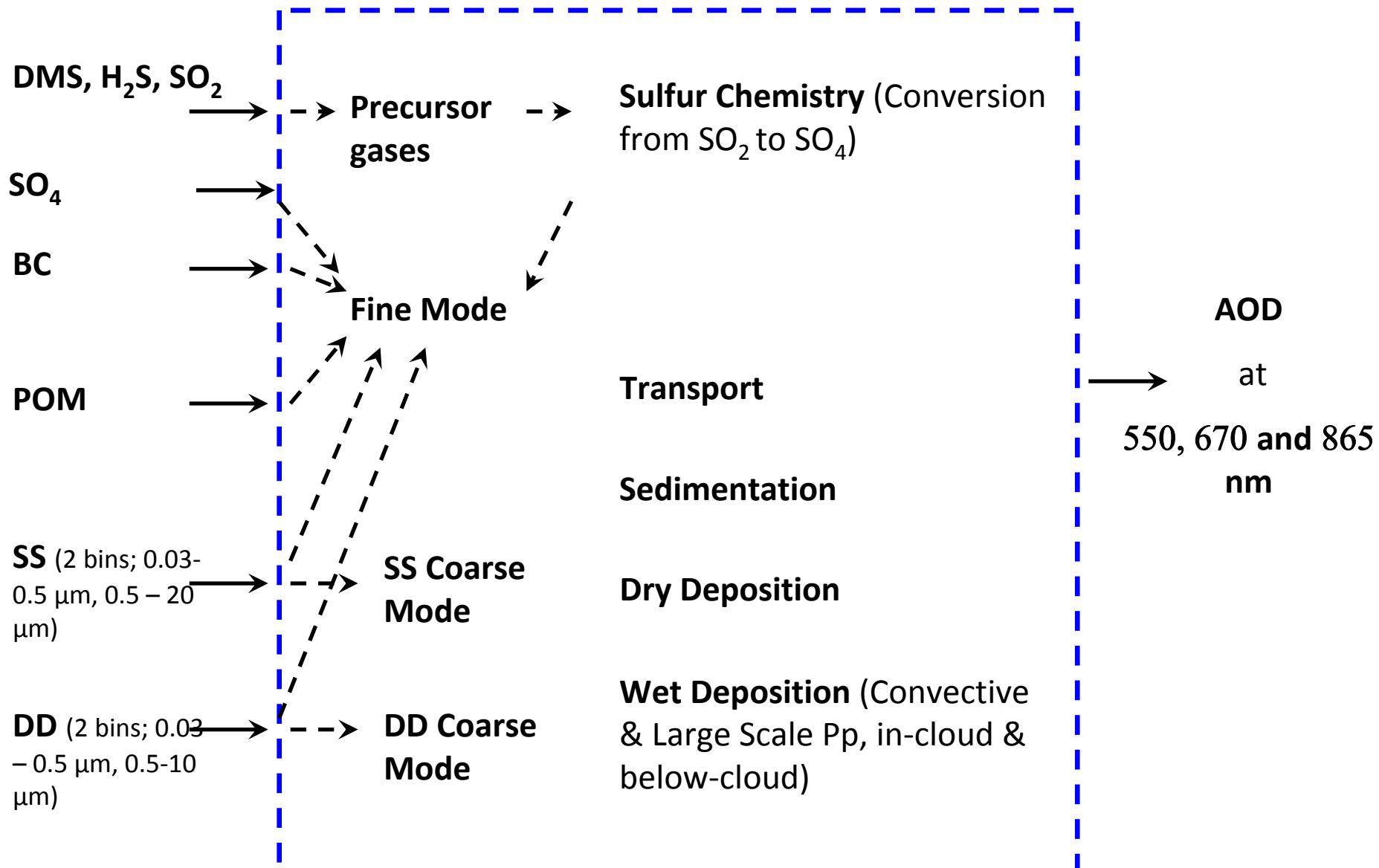
# LMDz 3.3.R



# LMDz 3.3.R

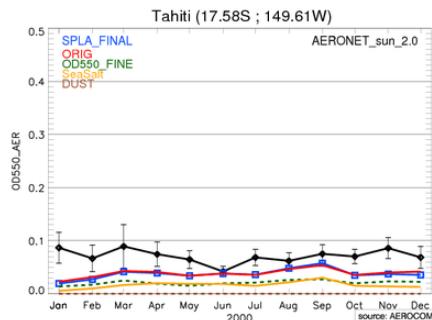
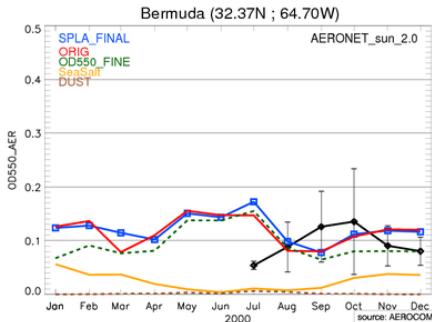
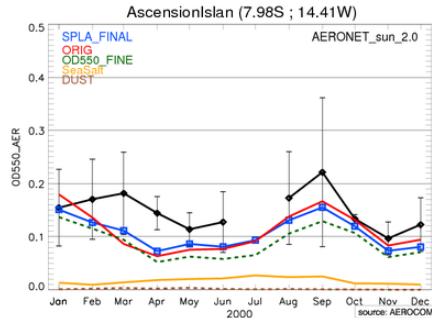


# Simplified Aerosol Model (SPLA)

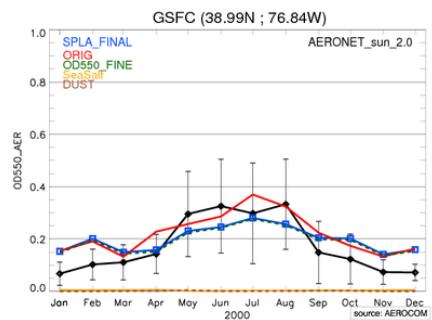
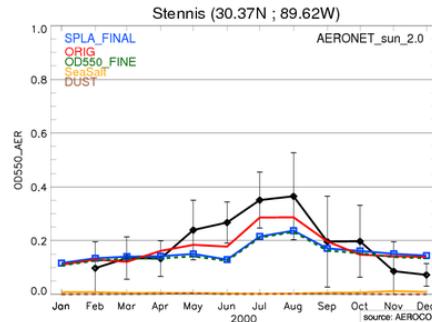
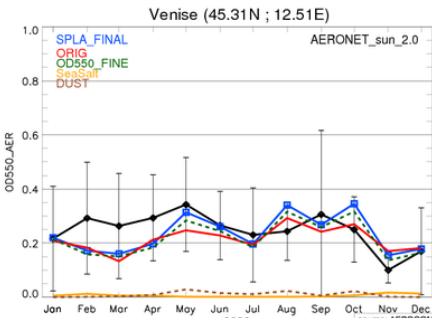


# Validation of SPLA (seasonal variability)

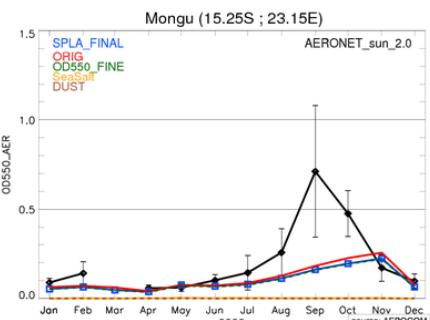
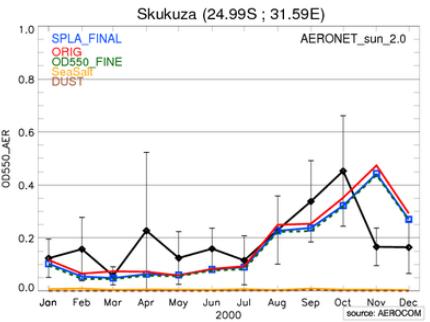
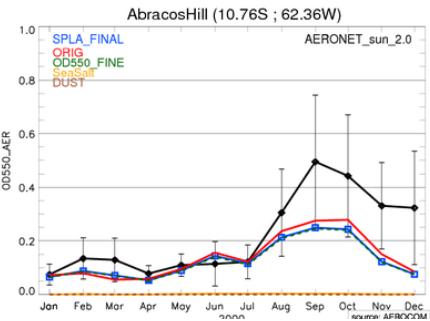
## Sea Salt Sites



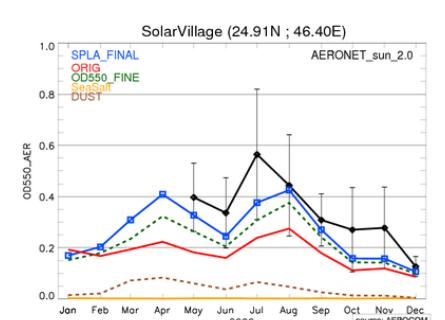
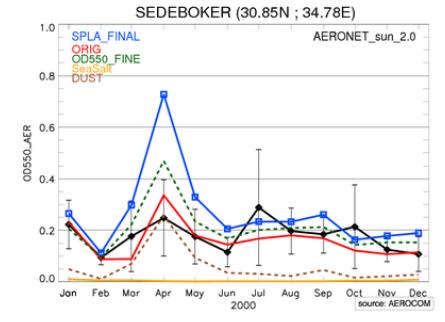
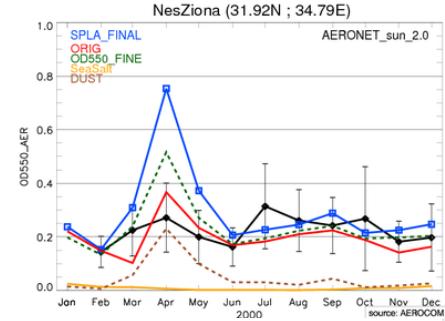
## Fossil Fuel Sites



## Biomass Burning Sites

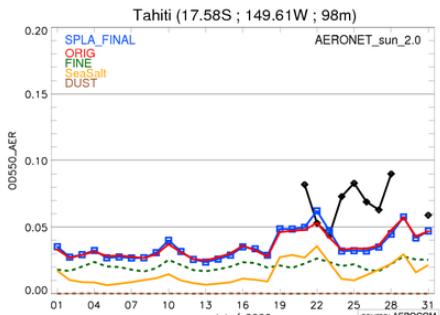
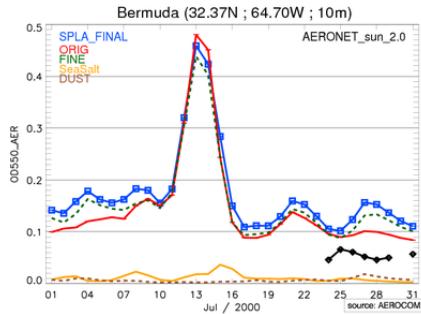
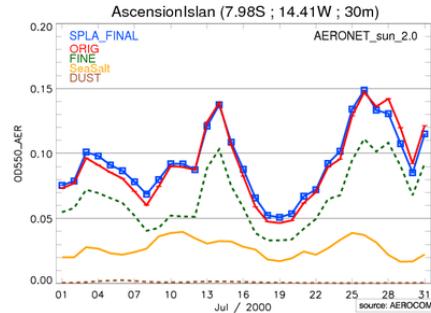


## Desert Dust Sites

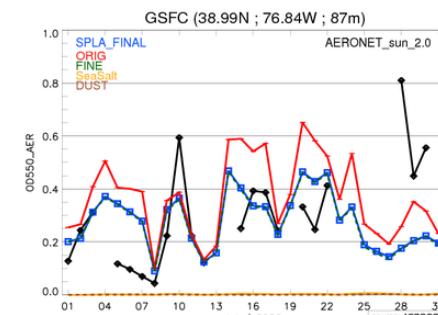
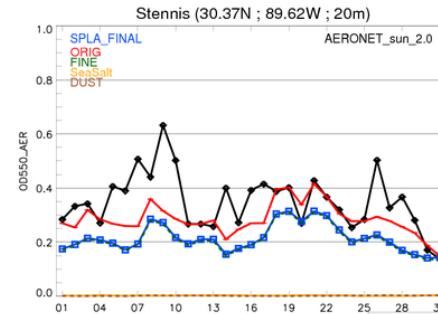
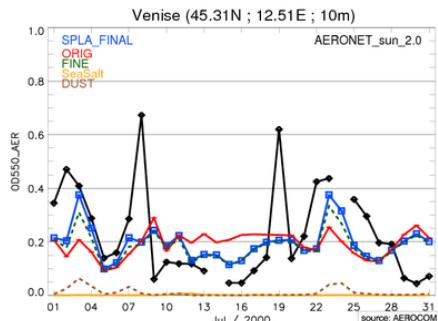


# Validation of SPLA (daily variability)

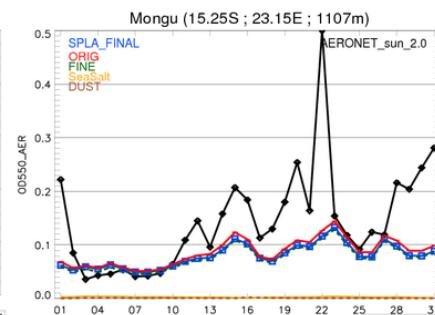
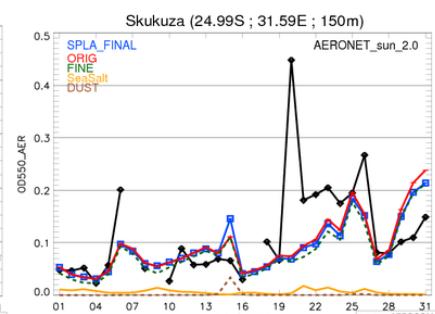
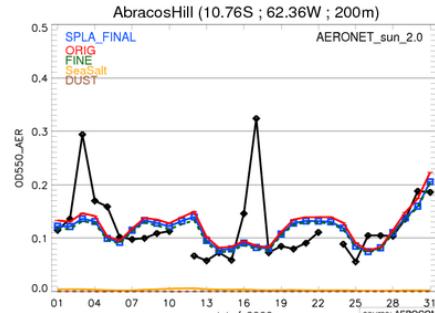
## Sea Salt Sites



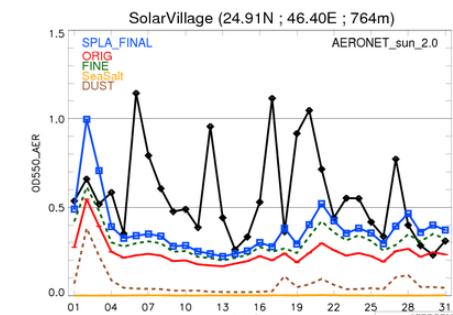
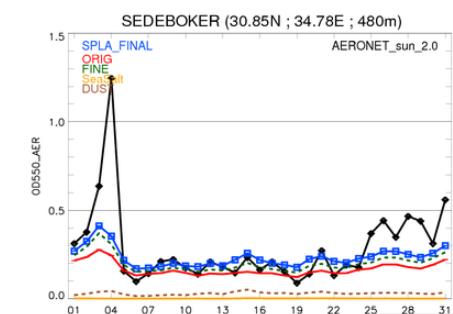
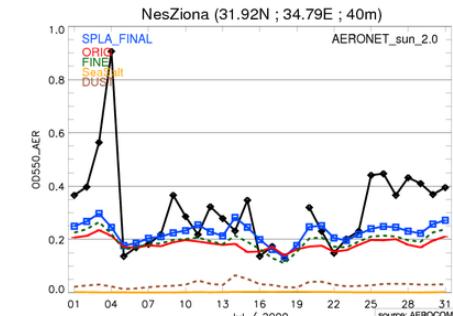
## Fossil Fuel Sites



## Biomass Burning Sites



## Desert Dust Sites



# Control Vector

Emission parameters defined by region :

- Sulfur Emissions (6)
- Biomass Burning (6)
- Combustion of fossil fuels (6)
- Sea salt fine & coarse (Global, 2)
- Desert dust fine & coarse (2x10)
- Conversion from sulfur to sulfate (5)

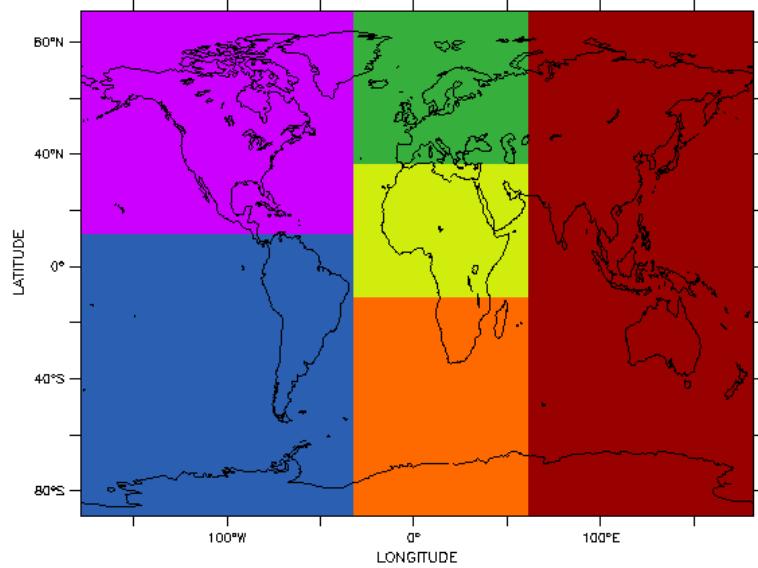
## « Observations » vector

Daily means of :

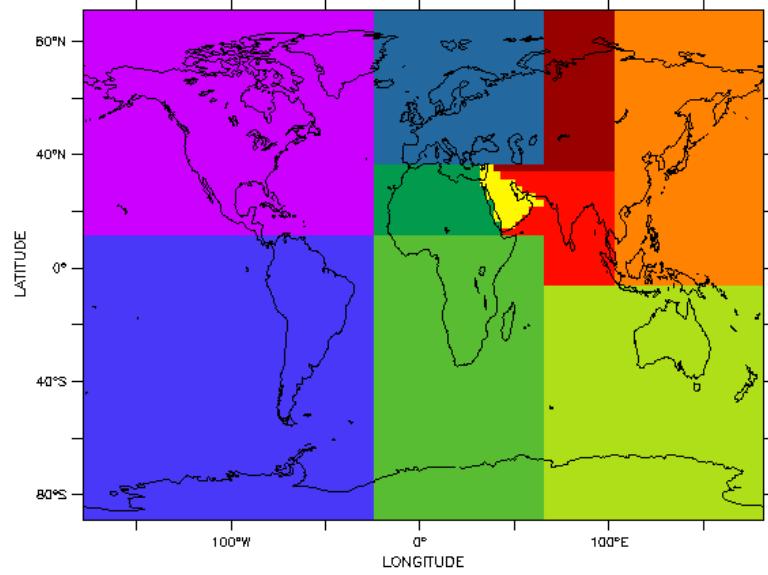
- MODIS total optical depth at 550 nm
- MODIS fine mode optical depth at 550 nm

# Emission Regions

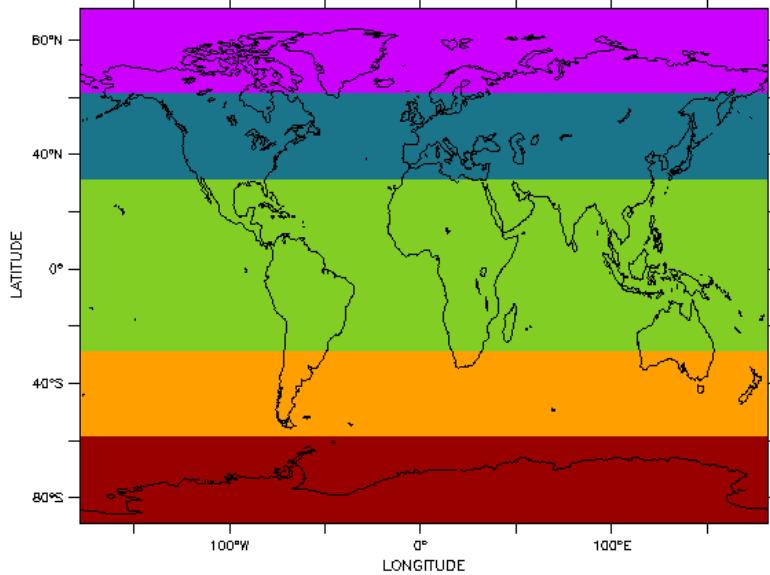
Fossil Fuel, Biomass Burning & Industrial Regions



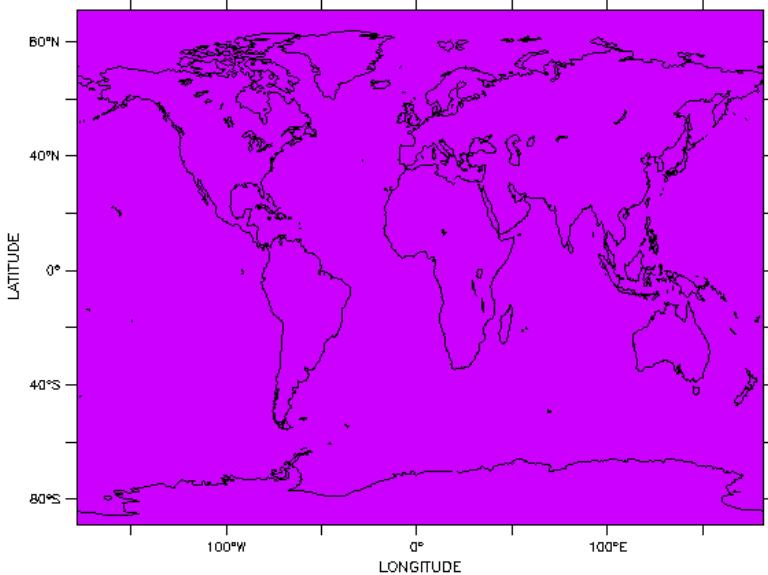
Dust Regions (Fine & Coarse)



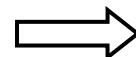
Chemistry Regions



Sea Salt Regions (Fine & Coarse)

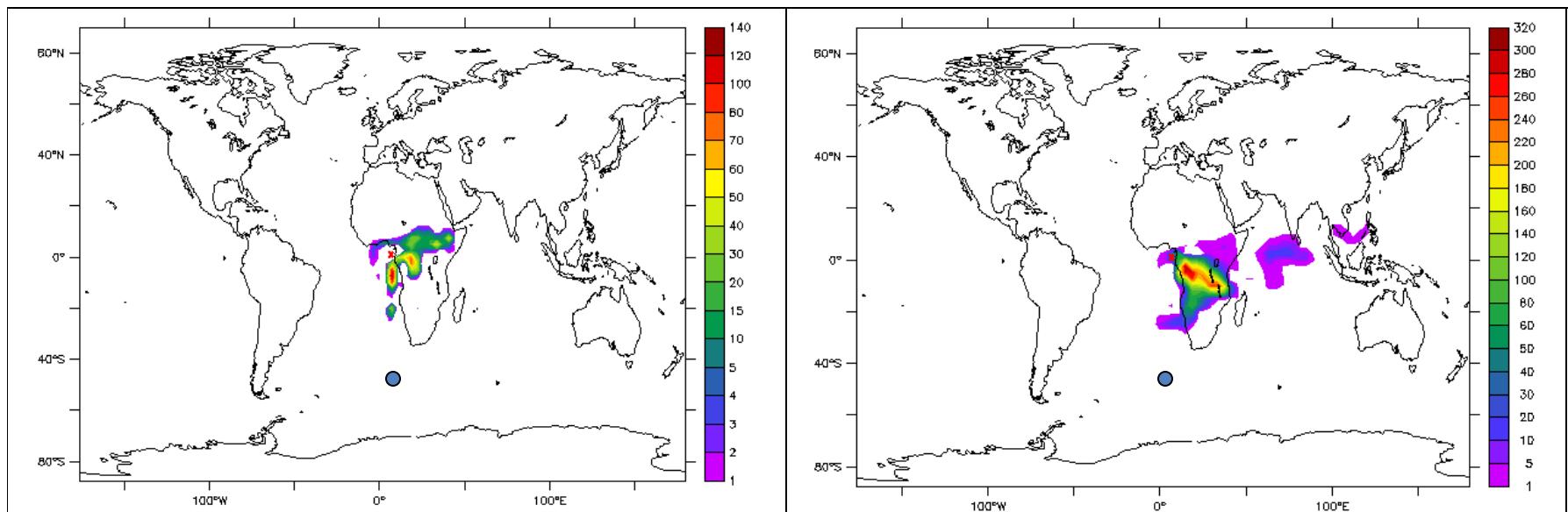


Adjoint of  
SPLA



Automatic differentiation  
TAPENADE

Adjoint : Perturbations in the input with respect to  
perturbations in the output



- 2 days

- 5 days

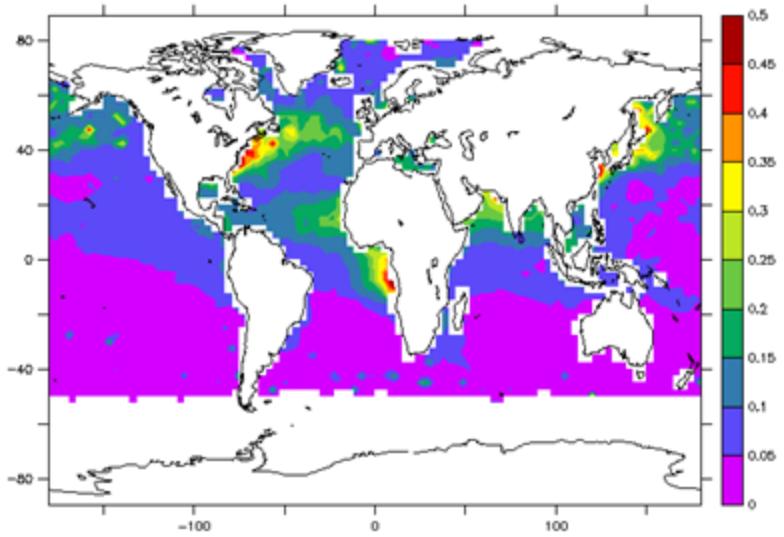
SPLA & Adjoint



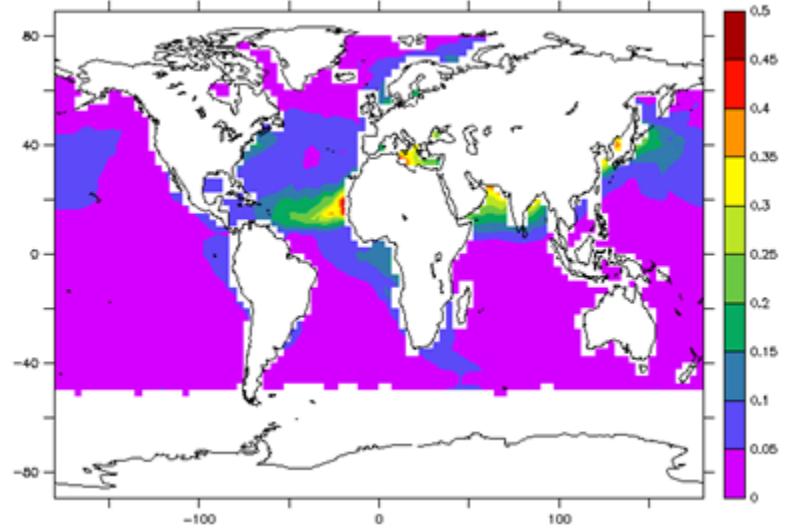
Global assimilation system used  
in estimation of gaseous  
emissions (Chevallier et al., 2005)

# Inversion

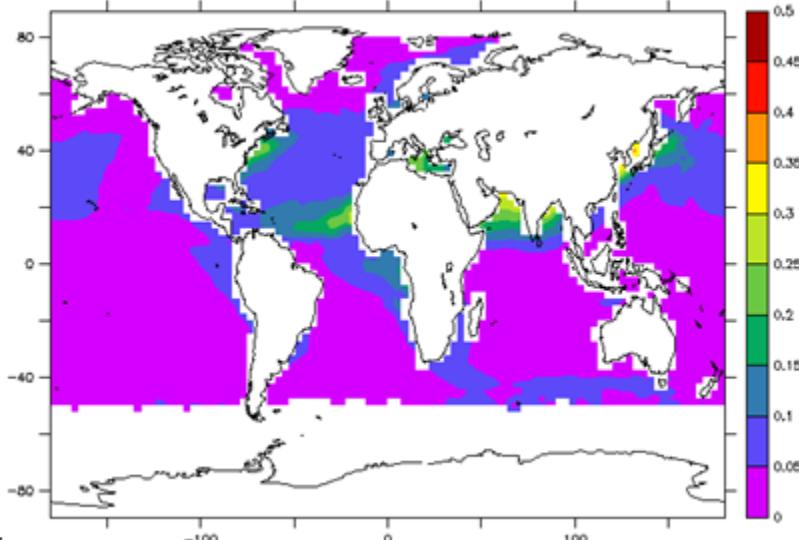
**Observations**



**A priori**



**Analysis**

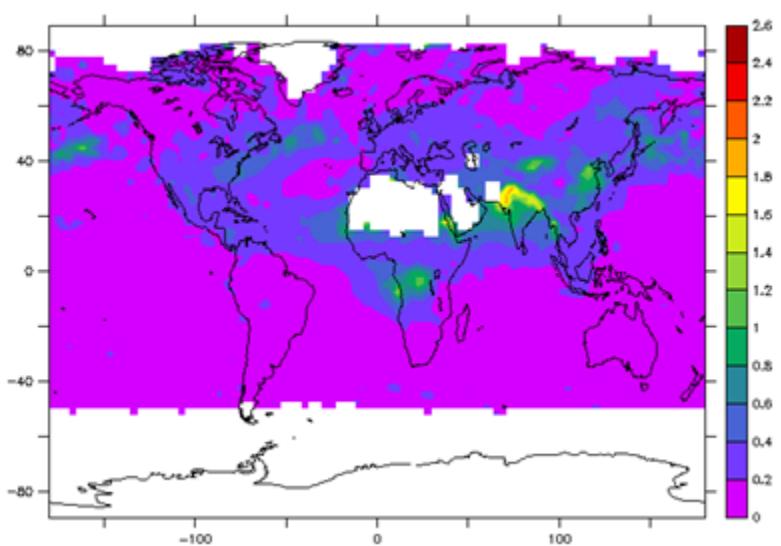


Fine mode AOD

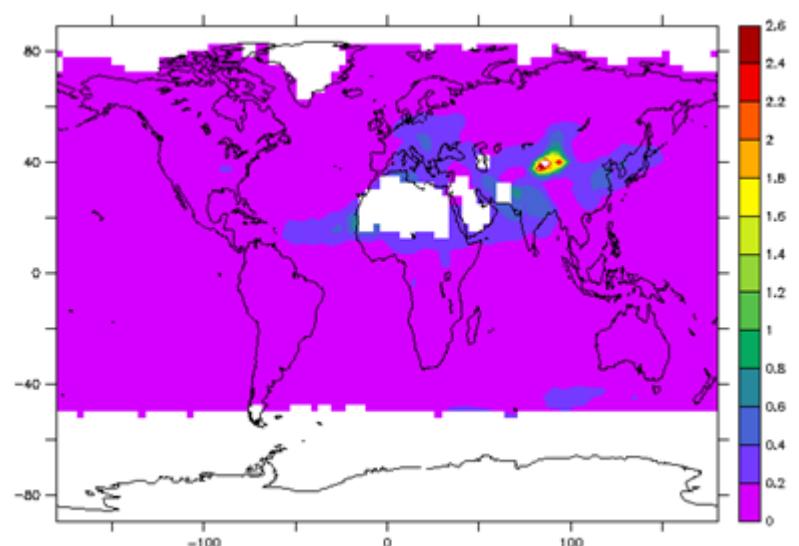
5 Iterations

# Inversion

**Observations**



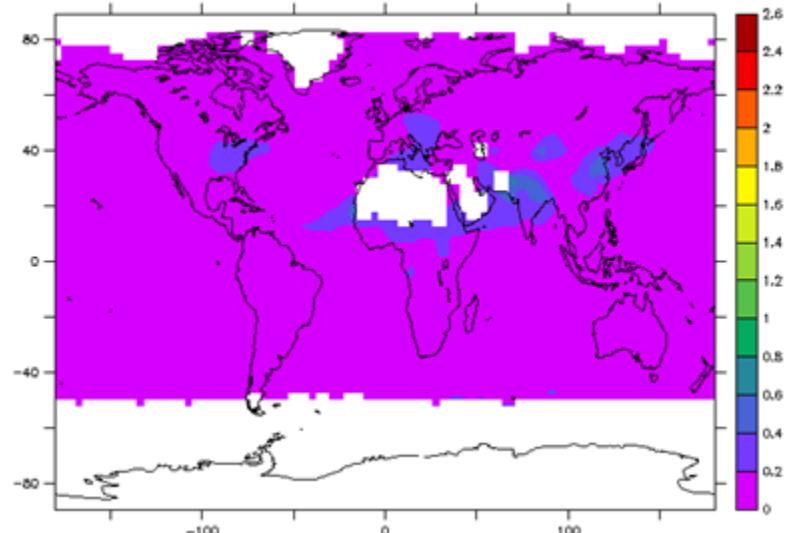
**A priori**



Total AOD

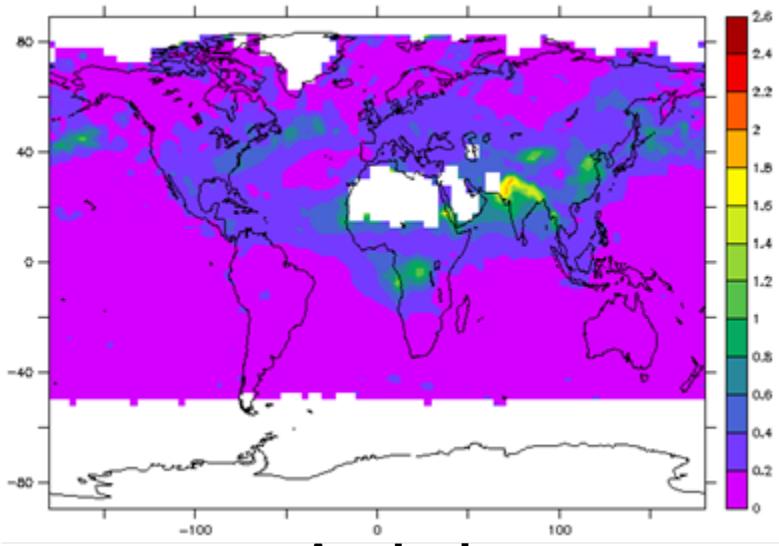
5 Iterations

**Analysis**

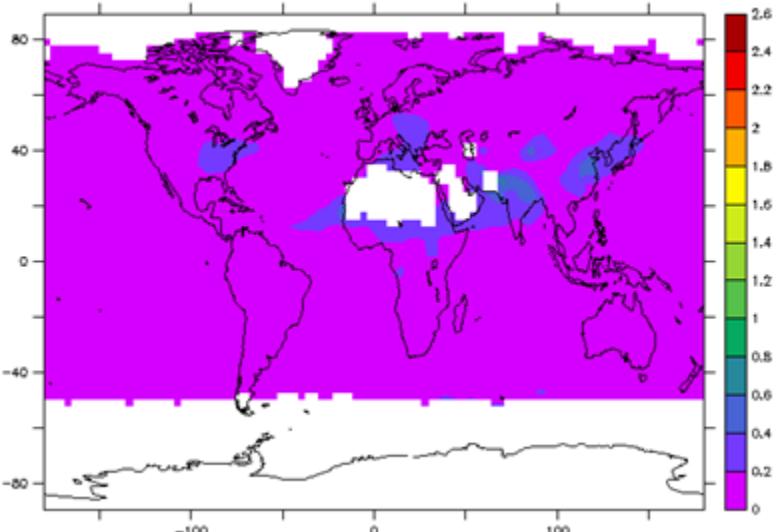


# Inversion - Total AOD

Observations



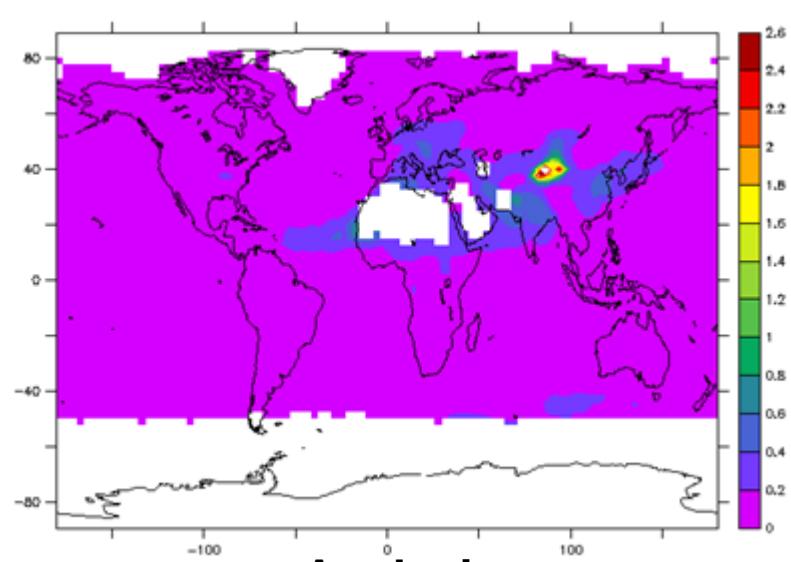
Analysis



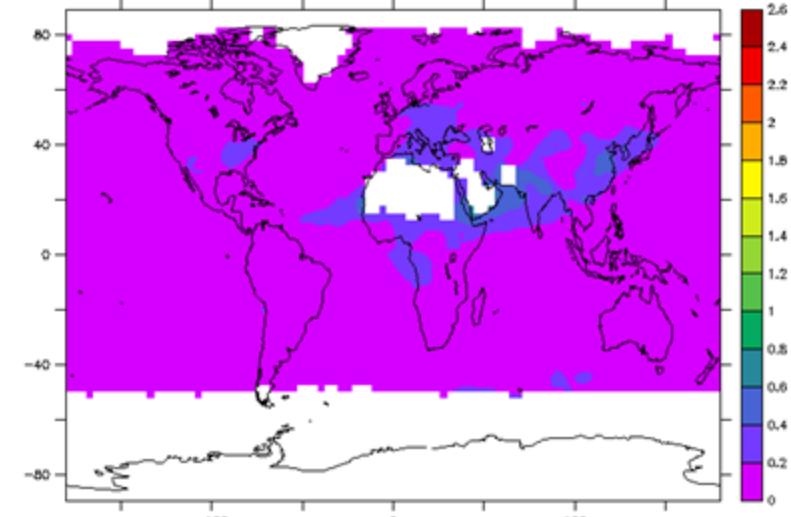
5 Iterations

8<sup>th</sup> AeroCom Workshop, Princeton, 5-7 October 2009

A priori



Analysis



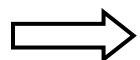
40 Iterations

## Direct Model

$$E_{\text{species}} = \sum_i S_i \times E_{\text{orig}}^i \quad i = \text{Aerosol species}$$

## Adjoint Model

$$S_i^* = S_i^* + E_{\text{orig}}^i \times E_{\text{species}}^*$$



**Definition of background error covariance matrix**

$$J = (x - x_b)^T \mathbf{B}^{-1} (x - x_b) + (y - \mathbf{H}[x])^T \mathbf{R}^{-1} (y - \mathbf{H}[x])$$

# Conclusions

- Derivation of a simplified model groupes 24 original species into 4
- Simplified model reproduces LMDz in monthly variability and is within the variability of AERONET
- More dificulties in reproducing the AERONET daily variability
- Introduced in global assimilation system
- Assimetry in the inversion

# Dust Intercomparison

- Definition of stations is now observation based
- Separating between dusty days and days with dust in mixture

$\alpha < 0.4$  Natural Aerosols

**Angstrom Exponent**  $\sim \alpha_0 + \tilde{\alpha}_1 M$  Mixture

$\alpha > 1.2$  Anthropogenic Aerosols

- Next step Paper