

Update on MODIS DT Pixel-Level Uncertainties

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Falguni Patadia (USRA/NASA GSFC)

Robert Levy (NASA GSFC)

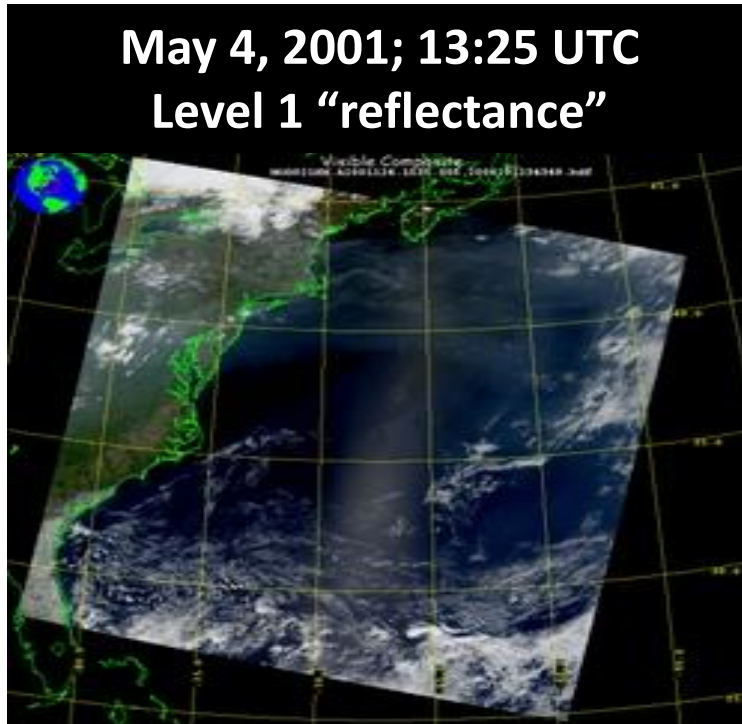
Shana Mattoo (SSAI/NASA GSFC)

Outline

- **DT Aerosol Retrieval**
- **Retrieval Challenges / Sources of Uncertainty**
- **Approaches to estimate uncertainty**
- **MODIS DT uncertainties**
- **Summary**

Aerosol retrieval from MODIS

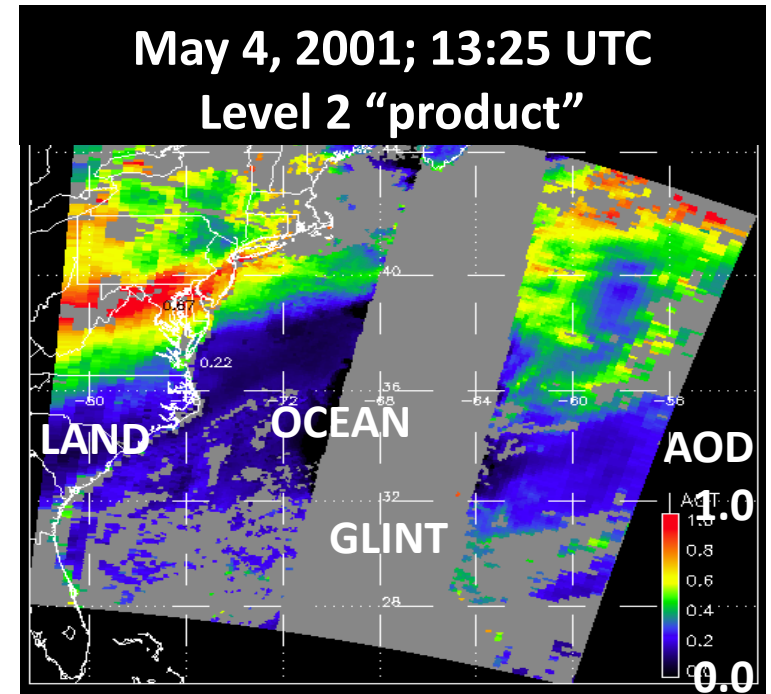
What MODIS observes



LUT



Attributed to aerosol (AOD)

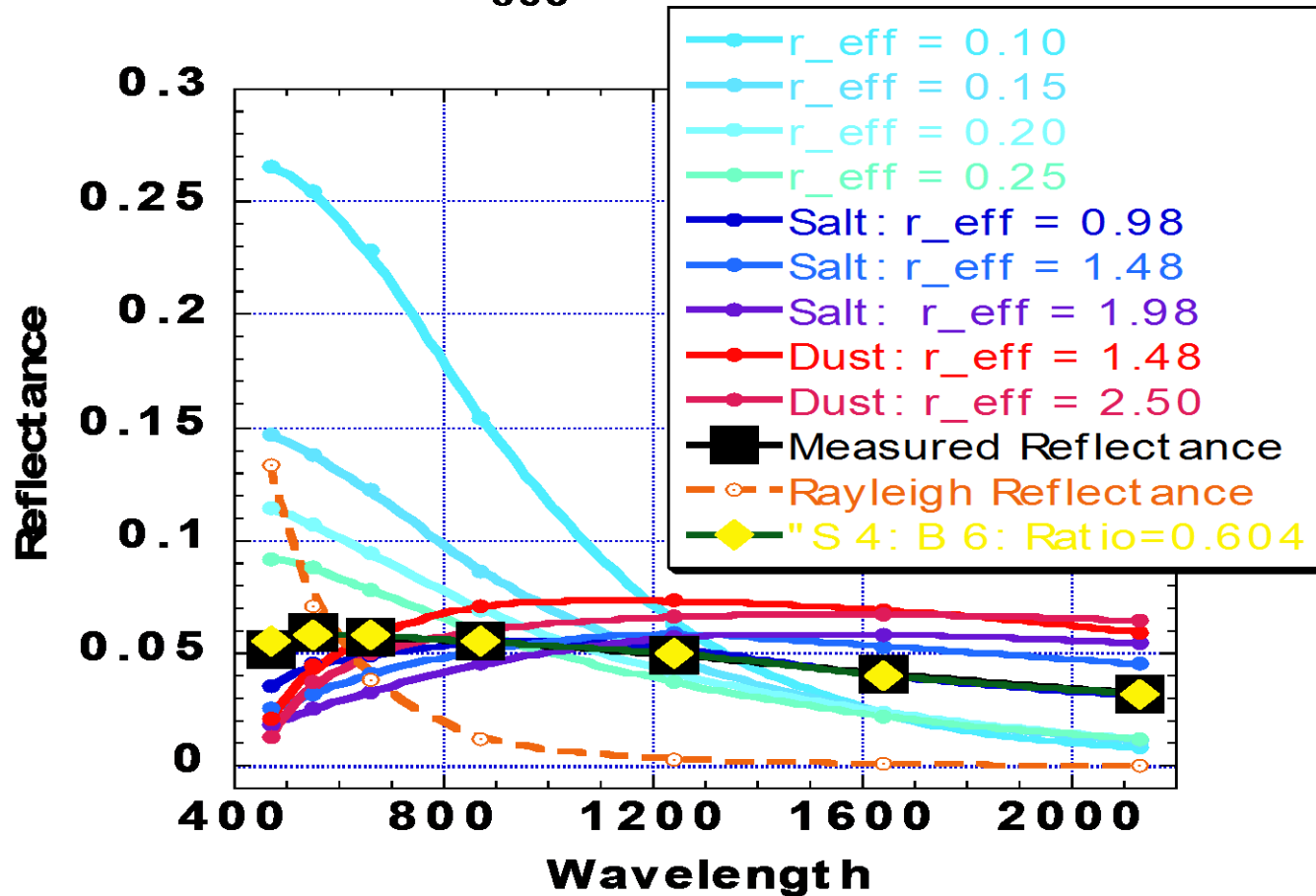


There are many different “algorithms” to retrieve aerosol from MODIS

1. Dark Target (“DT” ocean and land; Levy, Mattoo, Remer, Tanré, Kaufman)
2. Deep Blue (“DB” desert and beyond; Hsu, Bettenhausen, Sayer,..)
3. MAIAC (coupled with land surface everywhere; Lyapustin, Wang, Korokin,...)
4. Ocean color/atmospheric correction (McClain, Ahmad, ...)
5. Etc (neural net, model assimilation, statistical, ...)
6. Your own algorithm (many groups around the world)

MODIS Aerosol Retrieval – LUT Approach

Modeled and Observed Reflectance from MODIS
July 21, 14:50: $\tau_{865} = 0.48$



- Find a solution in the LUT that best matches the TOA spectral reflectance
- Then infer the aerosol conditions that produced the scene (e.g. AOD and size)

The Retrieval Challenge

Obtain estimates of
geophysical/optical quantities

Invert Observations (with noise)

Using RT / forward models (that
are not perfect)

And with (imperfect) prior
knowledge

Further complicated by non-
unique solutions

Major sources of uncertainties

Uncertainties in observations



Calibration

Uncertainties in data used to constrain retrievals



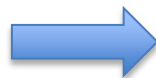
**Ancillary Data
(e.g. Ozone, WV used for atmospheric gas correction, WS)**

Retrieval Assumptions



**Surface reflectance,
aerosol models**

Uncertainties in forward model



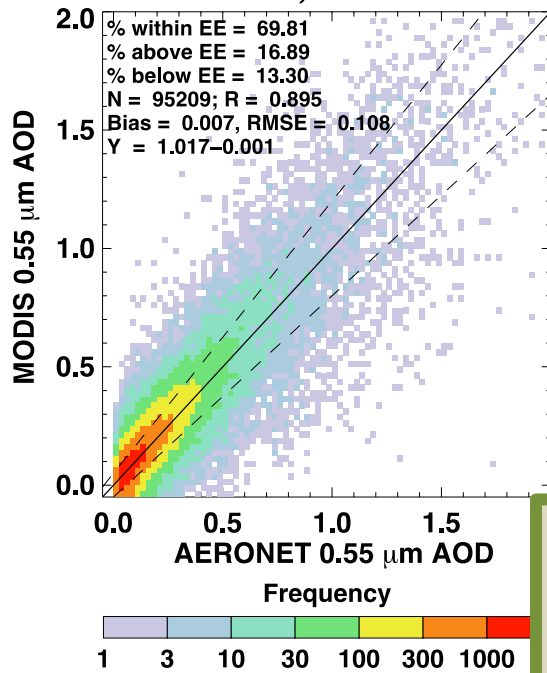
Non-Linearity

Multiple Approaches exist

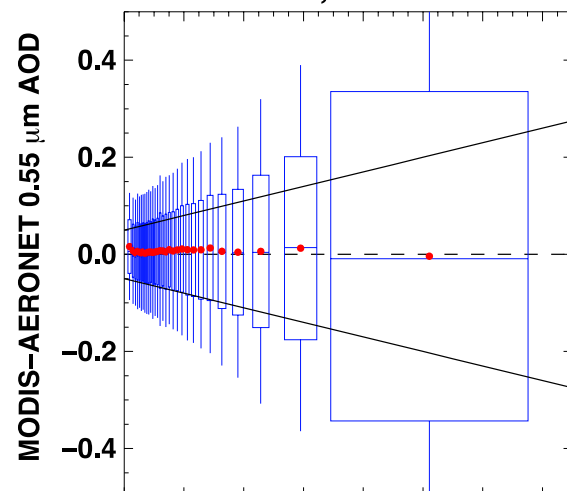
- **Validation (Error Envelope) – ground truth**
- **Per-pixel level uncertainty (error propagation)**
- **Ensemble retrievals to calculate dispersion in AOD**
 - **Which one makes sense for model?**
 - **Which one suffices ?**

Validation (Error Envelope)

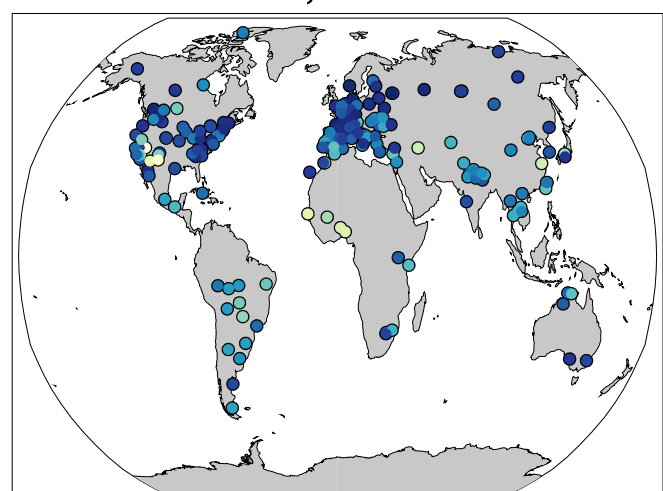
C6 Land, 2002–2014



C6 Land, 2002–2014

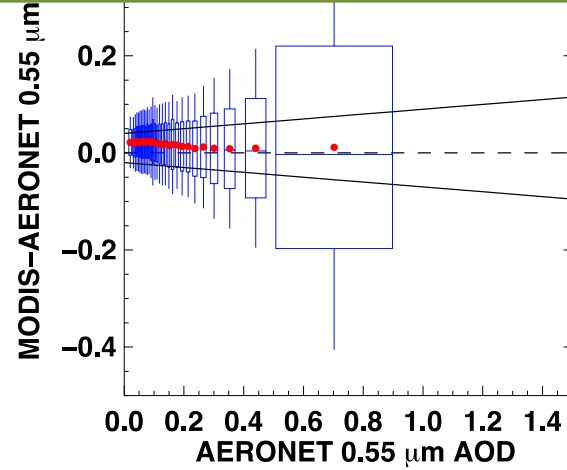
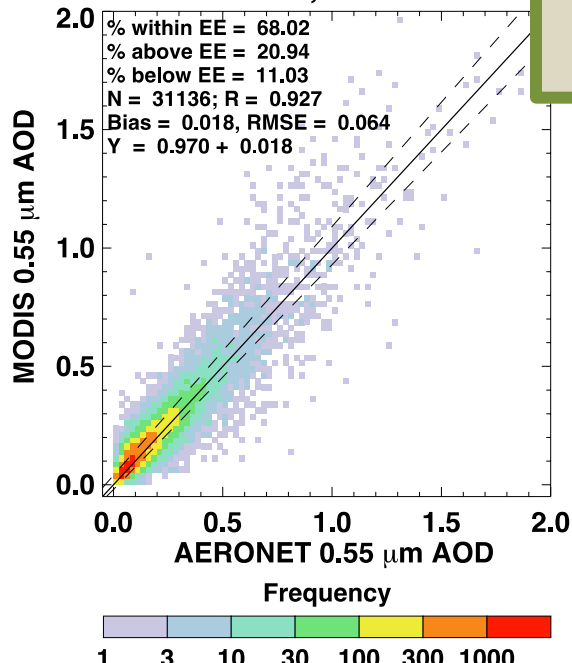


C6 Land, 2002–2014

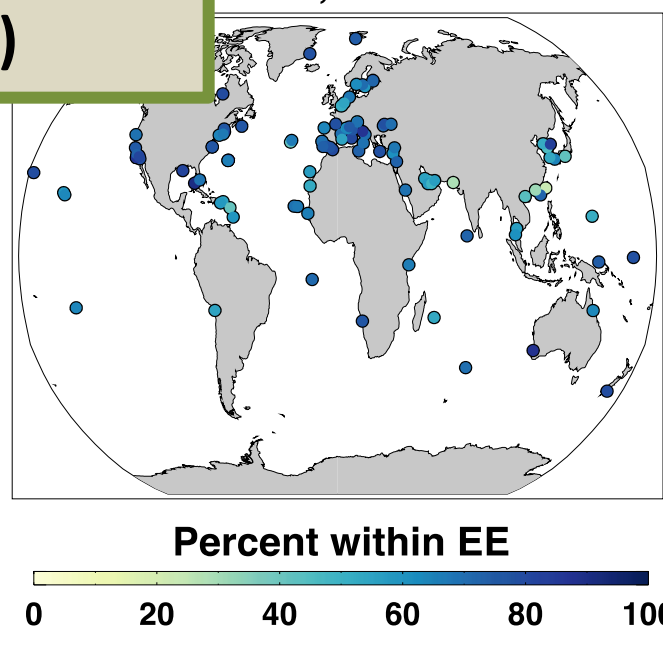


– Ocean : $\pm(0.03 + 10\% * \tau_A)$
 – Land : $\pm(0.05 + 15\% * \tau_A)$
 (About 68% within EE)

C6 Ocean, 2002–2014



C6 Ocean, 2002–2014



Error Propagation

Definitions and Methodology

For a 2-channel retrieval scheme, the change in retrieved aerosol optical depth due to change in some parameter 'a' can be written as:

$$D t_{,} = \frac{\partial t}{\partial R1} \Big|_{R2} \frac{dR1}{da} Da + \frac{\partial t}{\partial R2} \Big|_{R1} \frac{dR2}{da} Da + \dots \quad \dots (1)$$

where :

- * R1 and R2 = TOA aerosol reflectance in two spectral channels
- * **a** = the source of uncertainty i.e. measurement / calibration error, atmospheric correction error, surface reflectance error etc.
- * Partial derivative of τ = the retrieval sensitivity of τ [can be compute from LUT]

Equation (1) can be written as :

$$D t_{,} = \frac{\partial t}{\partial R1} \Big|_{R2} DR1 + \frac{\partial t}{\partial R2} \Big|_{R1} DR2 + \dots \quad \dots (2)$$

ΔR can be calculated for various error sources

Definitions and Methodology

The Retrieval Error can be written in Matrix Form as : $\mathbf{K}^{-1} \mathbf{O} (\mathbf{K}^{-1})^T$ OR $\mathbf{S} \mathbf{O} \mathbf{S}^T$

where ,

$$\mathbf{S} = \mathbf{K}^{-1}$$

$$\mathbf{K} = \text{Partial derivative} \left(\frac{\partial t}{\partial R} \right)$$

\mathbf{O} = Uncertainty Covariance (ΔR) Matrix

For 7-Channel MODIS-DT Over Ocean Retrieval,

$$\mathbf{S} = \begin{bmatrix} \frac{\partial R1}{\partial t} \\ \frac{\partial R2}{\partial t} \\ \cdot \\ \cdot \\ \cdot \\ \frac{\partial R7}{\partial t} \end{bmatrix}$$

$$\mathbf{O}_{\text{atmos_error}} = \begin{bmatrix} S_{DR1}^2 & \dots & S_{DR1DR7} \\ \cdot & & \cdot \\ \cdot & S_{DR2}^2 & \cdot \\ \cdot & & \cdot \\ S_{DR1DR7} & \dots & S_{DR7}^2 \end{bmatrix}$$

Brute Force Calculations

Brute Force Approach

Retrieve AOD Three times using (3 Runs)

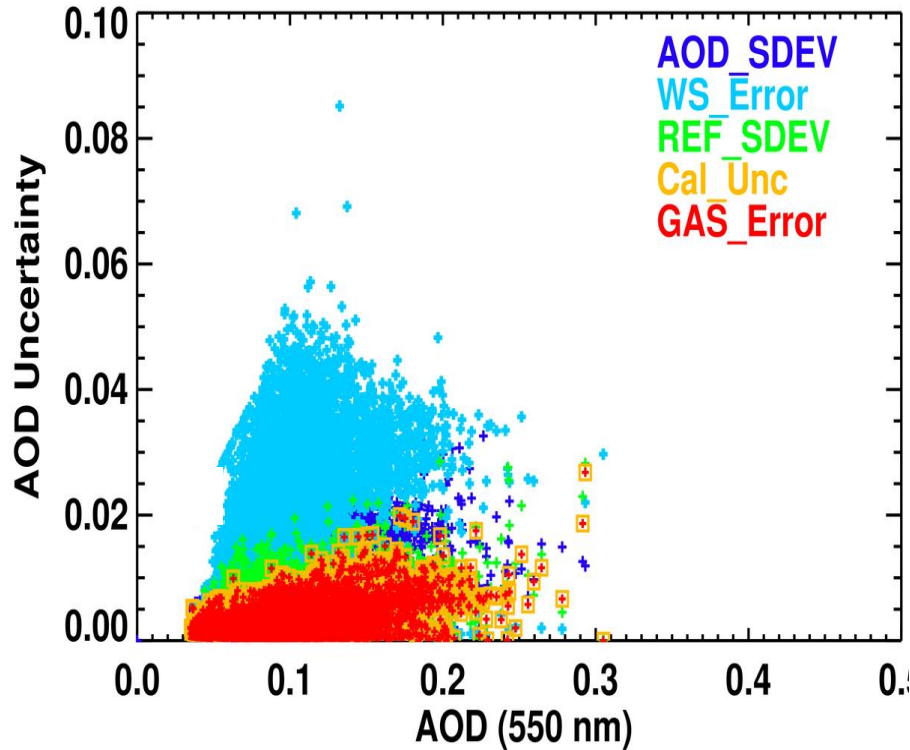
For Example:

- (a) 10 km mean reflectance (ρ_λ) used in standard retrieval
- (b) ρ_λ plus standard deviation in 10 km reflectance [$\rho_\lambda + \sigma_\lambda$]
- (c) ρ_λ minus standard deviation in 10 km reflectance [$\rho_\lambda - \sigma_\lambda$]

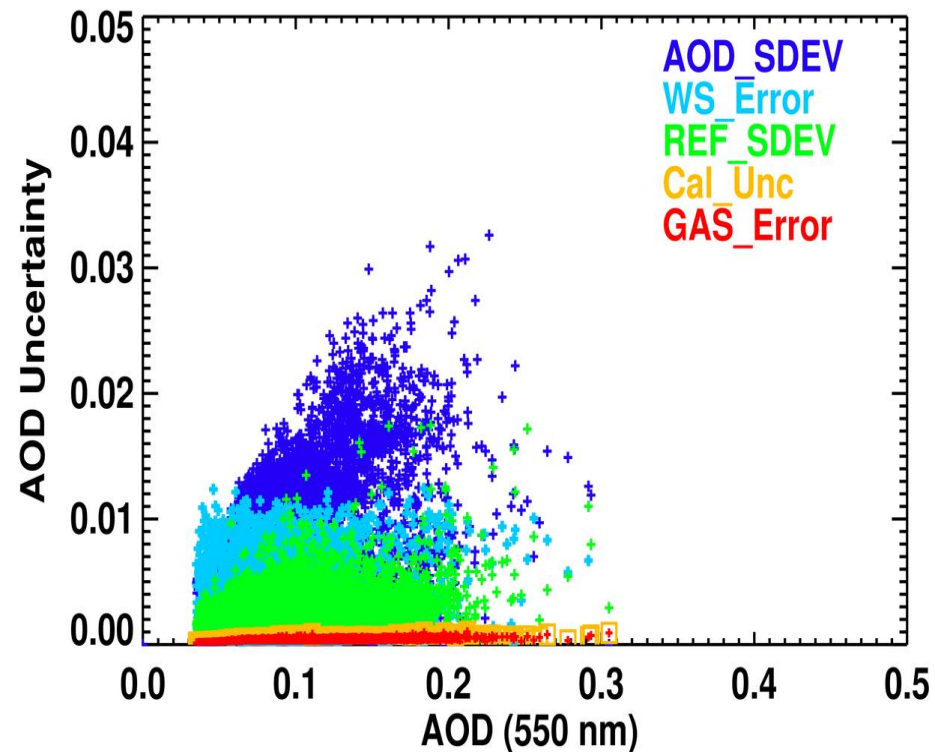
Calculate uncertainty / standard deviation in AOD from these 3 calculations

Summary Plot : Uncertainty in AOD retrieval

(a) Brute Force Method



(b) Jacobian Method



- Uncertainty from the aerosol models (AOD_SDEV) dominates (Jacobian)
- Atmospheric gas correction errors lowest
- **What do these uncertainty numbers mean? How do magnitudes compare with EE ? (<15%)**

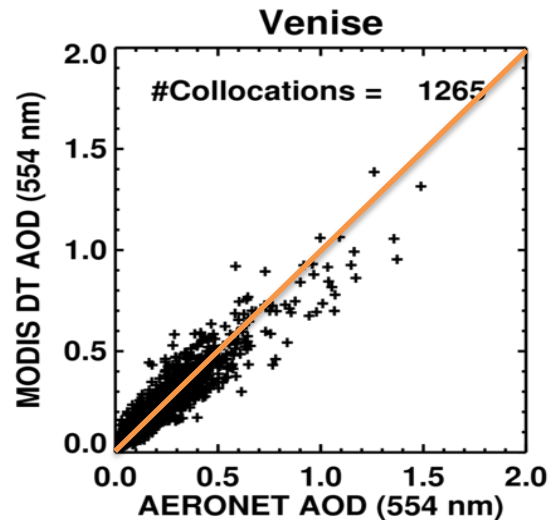
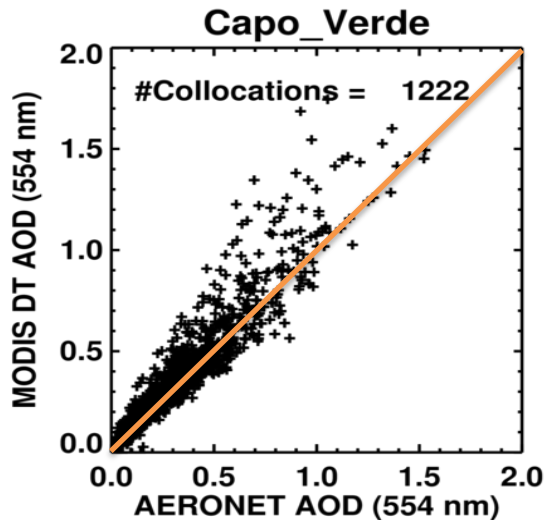
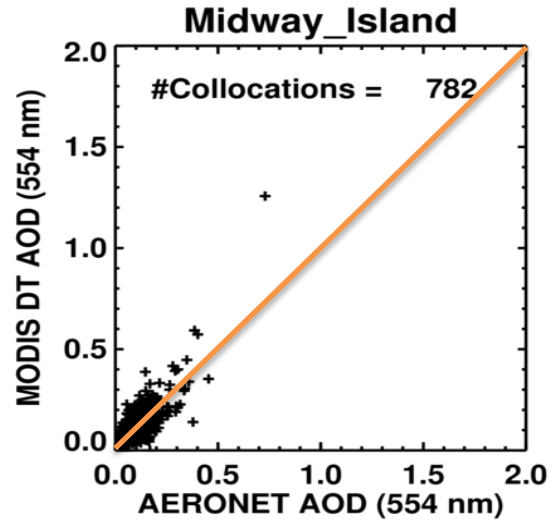
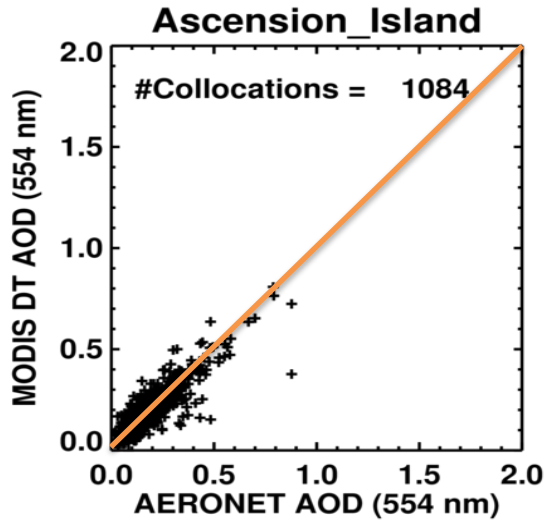
Asking this question

Do **AOD uncertainties** from different approaches **converge within** the error / **uncertainty envelopes** ? [if errors are calculated in a consistent way?]

Inter-compare Uncertainty in DT AOD retrieval : The 3 approaches



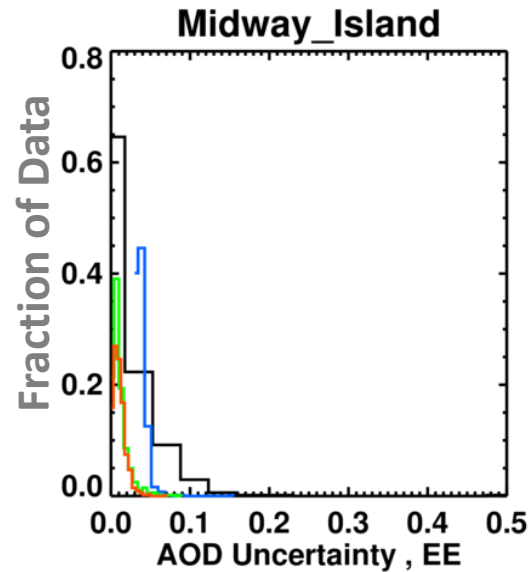
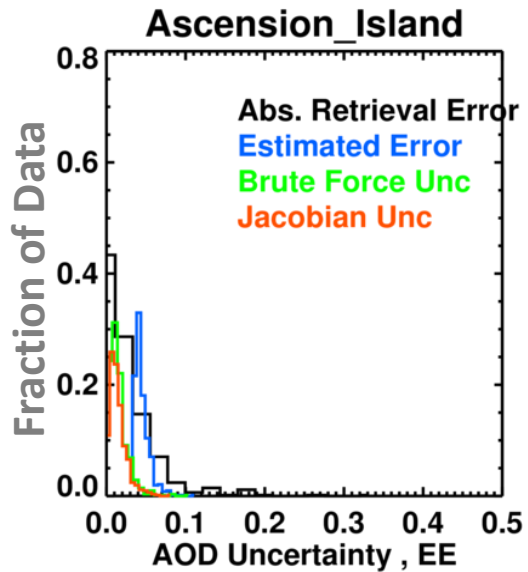
MODIS DT C6 AOD (Terra+Aqua) over 4 Ocean Sites : 2000 – 2017



Collocation Criteria

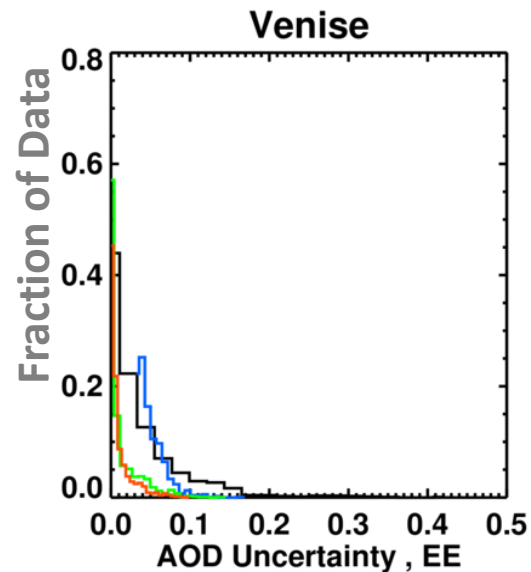
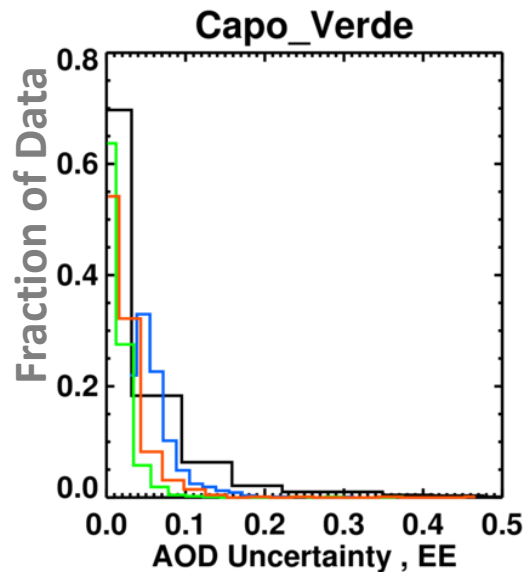
- Nearest retrieval within 25 km of site
- At least 5 retrievals in one year

Comparison of Uncertainty in DT AOD retrieval with Retrieval Error



Retrieval Error = MODIS - AERONET AODs

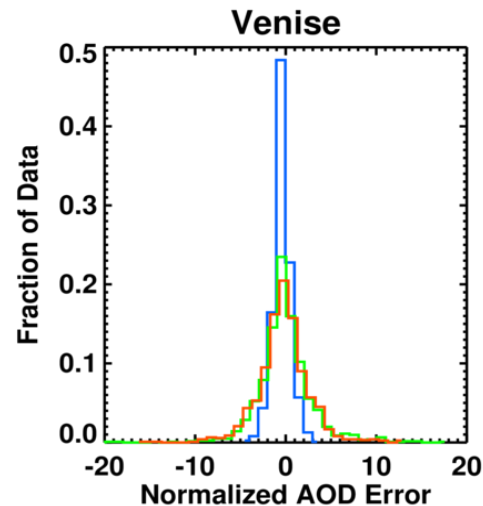
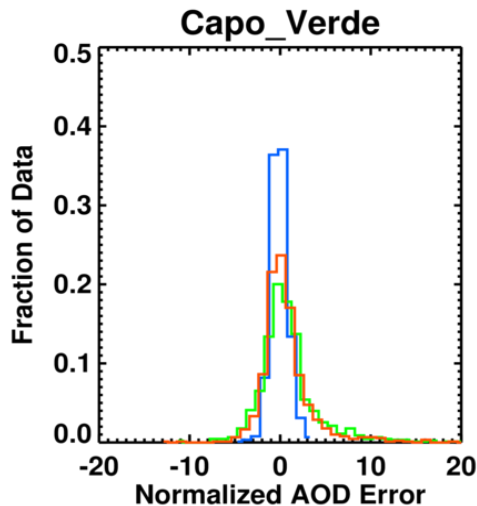
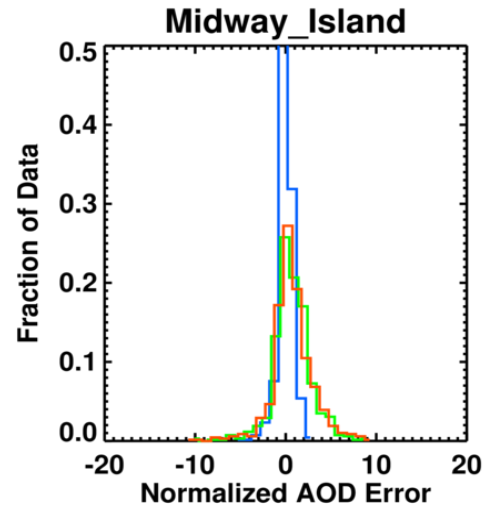
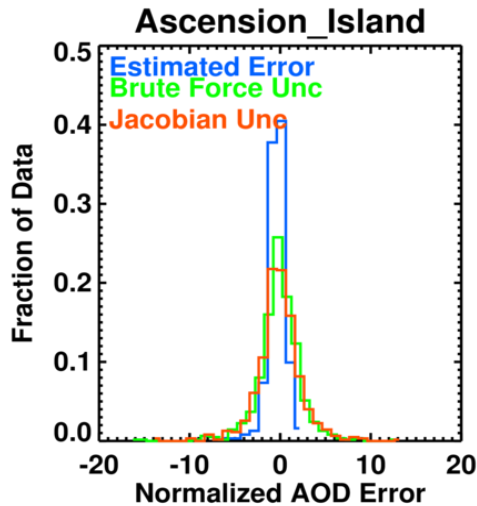
Estimated Error = $\pm(0.03 + 10\% * \tau_A)$



Error Propagation < Retrieval Error

Although site dependent, uncertainties computed from error propagation or ensemble of retrievals are smaller than the retrieval error

Normalized Errors : Both AERONET & Retrieval Uncertainty



Normalized Error = Retrieval Error /
Estimated Difference (ED)

$$ED = [(\text{retrieval uncertainty})^2 + (\text{AERONET uncertainty})^2]$$

- Retrieval Error larger than Brute force , Jacobian Uncertainties
- Error propagation (with known error sources) helps define the precision of retrievals
- Understanding the sources of (in)accuracy of retrieval requires in-situ observations

Retrievals in cloud vicinity compromises the comparisons against AERONET

Conclusion/Summary

- The MODIS dark-target aerosol retrieval and products is maturing
- Prior to MODIS launch, we performed sensitivity tests to derive expected error (EE) envelopes
- Post launch, these EE envelopes for AOD was “validated” by comparing to sun-photometer data
- Later on, as N increased, new sites with new surface and aerosol characteristics were added
- The EE envelope was revised to meet the performance compared to all global sites
- But some retrievals are better or worse than EE
- We know that
- **Quality flags (=1,2,3 Ocean) gives best retrieval – to increase N, quantitative uncertainty estimates can be helpful**
- Hopefully we can work with AeroSAT & CCI project and do this consistently.